

Discrete choice (1)

Applied Econometrics for Spatial Economics

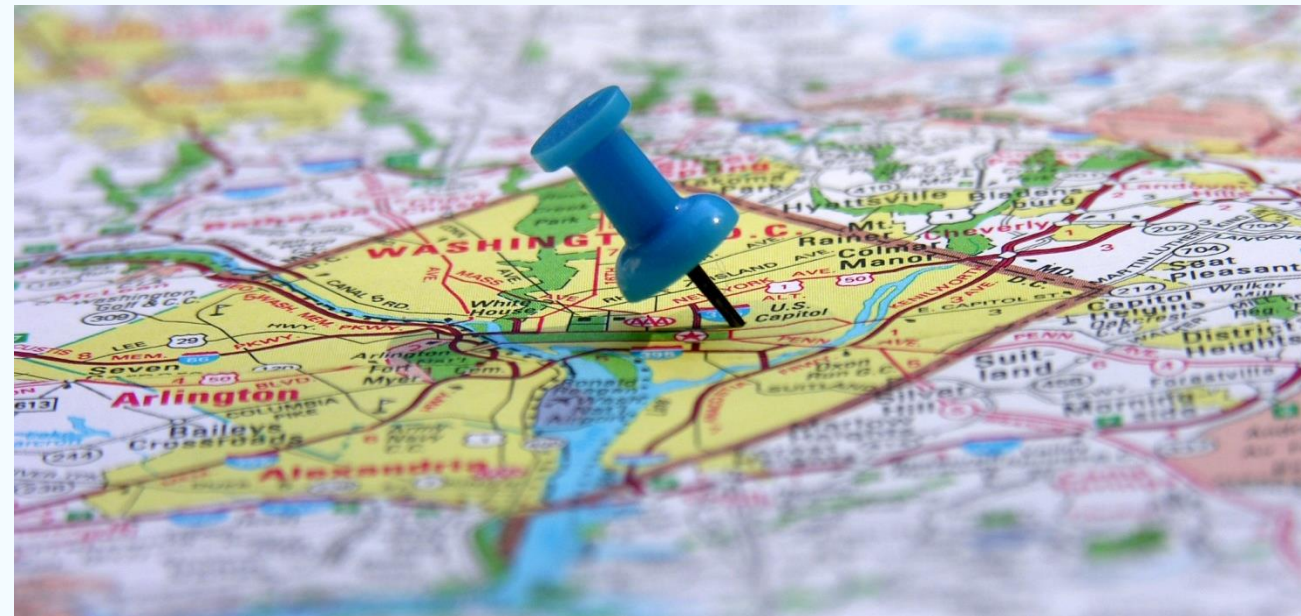
Hans Koster

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1. Introduction
2. The RUM framework
3. Value of time
4. Multiple alternatives
5. Summary



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- **If you have data at your disposal you may use these data to answer practical questions:**
 - **What factors influence the carrier's selection of a port?**
 - **Which mode do people prefer to travel from A to B?**
 - **Where do people want to live?**

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- ***Continuous* choice: estimate marginal changes in behaviour**
 - E.g. “when fuel price increases by 10%, the demand for fuel will decrease by 2%”
 - Standard micro-economic theory applies

- **Transport demand often has a discrete (binary) nature**
 - Some x impacts a discrete y
 - Then use discrete choice methods

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- **Discrete choice methods**
 - *Dependent variable y_i is discrete*
- **Why not use OLS?**
- **Let's have the standard OLS equation**

$$y_i = \beta x_i + \epsilon_i \quad (1)$$

where i indexes the individual

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- **OLS may be consistent for binary choice**
 - *But, y_i (and therefore ϵ) is not normally distributed*

- **Horrace and Oaxaca (2006)**
 - Leads to biased and inconsistent estimates if \hat{y}_i lies 'often' outside the $[0,1]$ interval
 - I show in Clip #9 why that is an issue...

- **OLS does not necessarily provides a link with economic theory**

- **Not suitable for multinomial choice**

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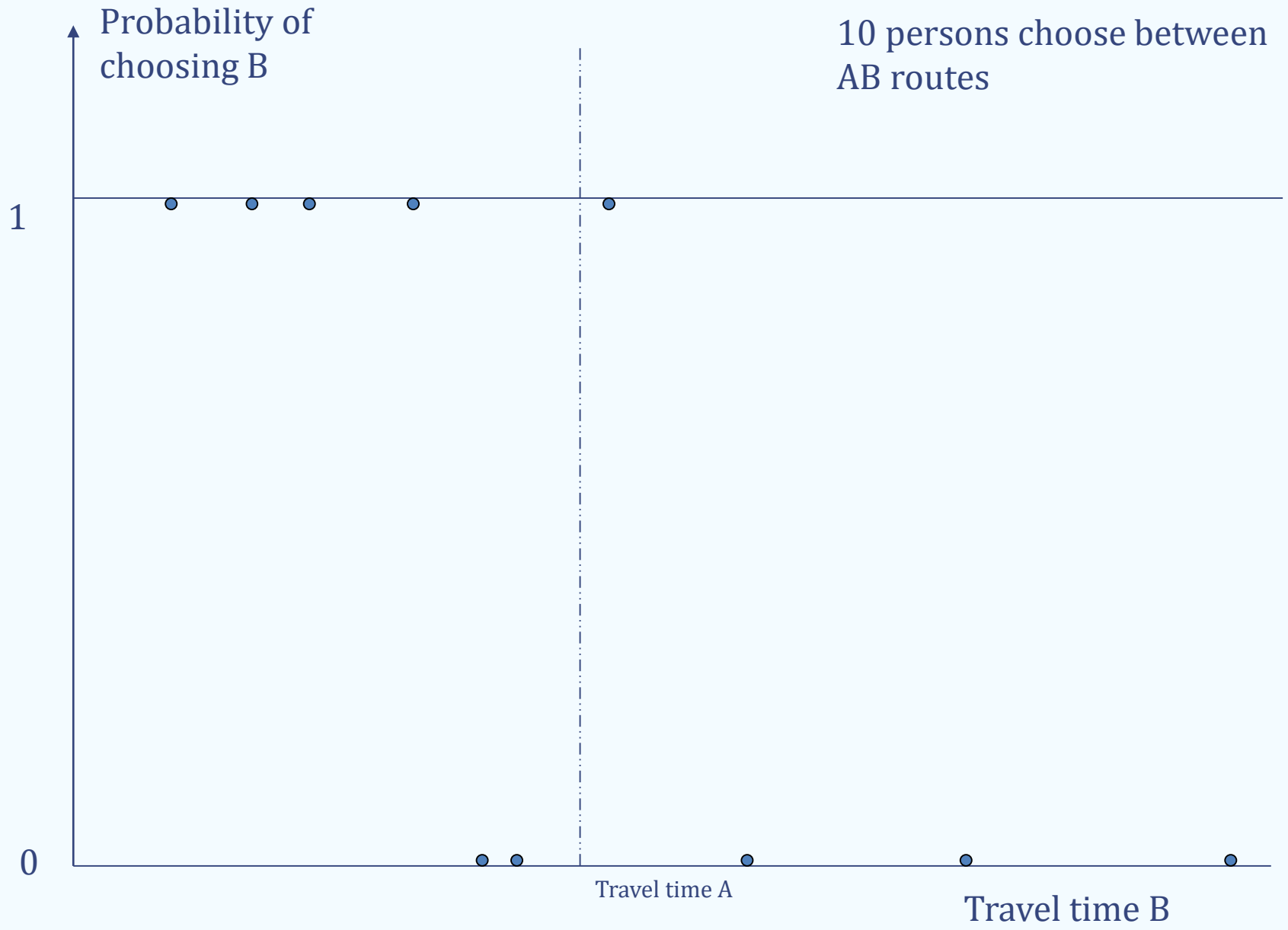
- **This week**
 - **Learn about how to deal with discrete choices**
 - **... and stated choice experiments**

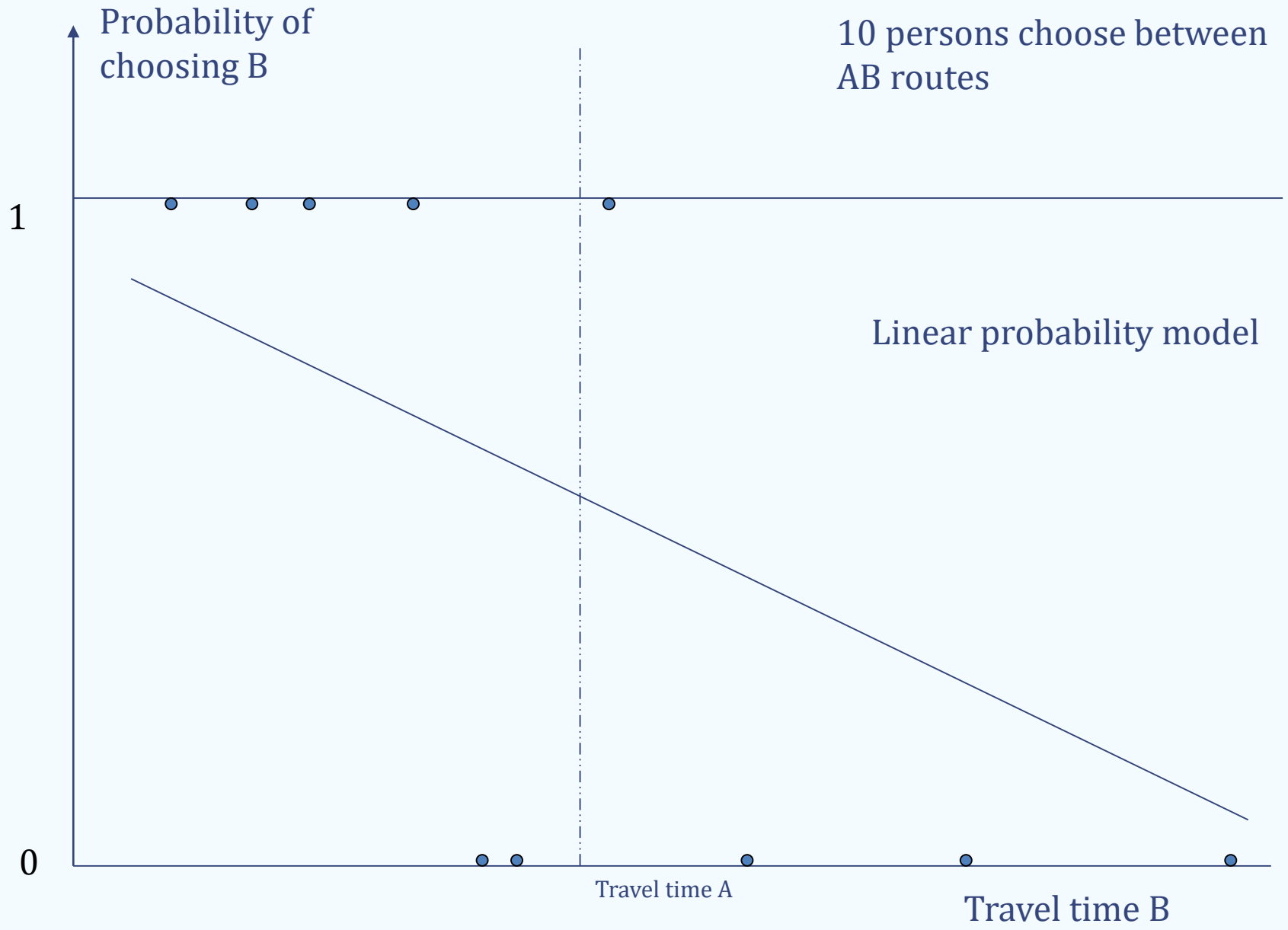
- **Plan:**
 - Lecture #1: The random utility framework**
 - Lecture #2: Estimating binary choice models**
 - Lecture #3: Estimating multinomial choice models**
Stated vs. revealed preference data
 - Assignment: Estimate the value of time**

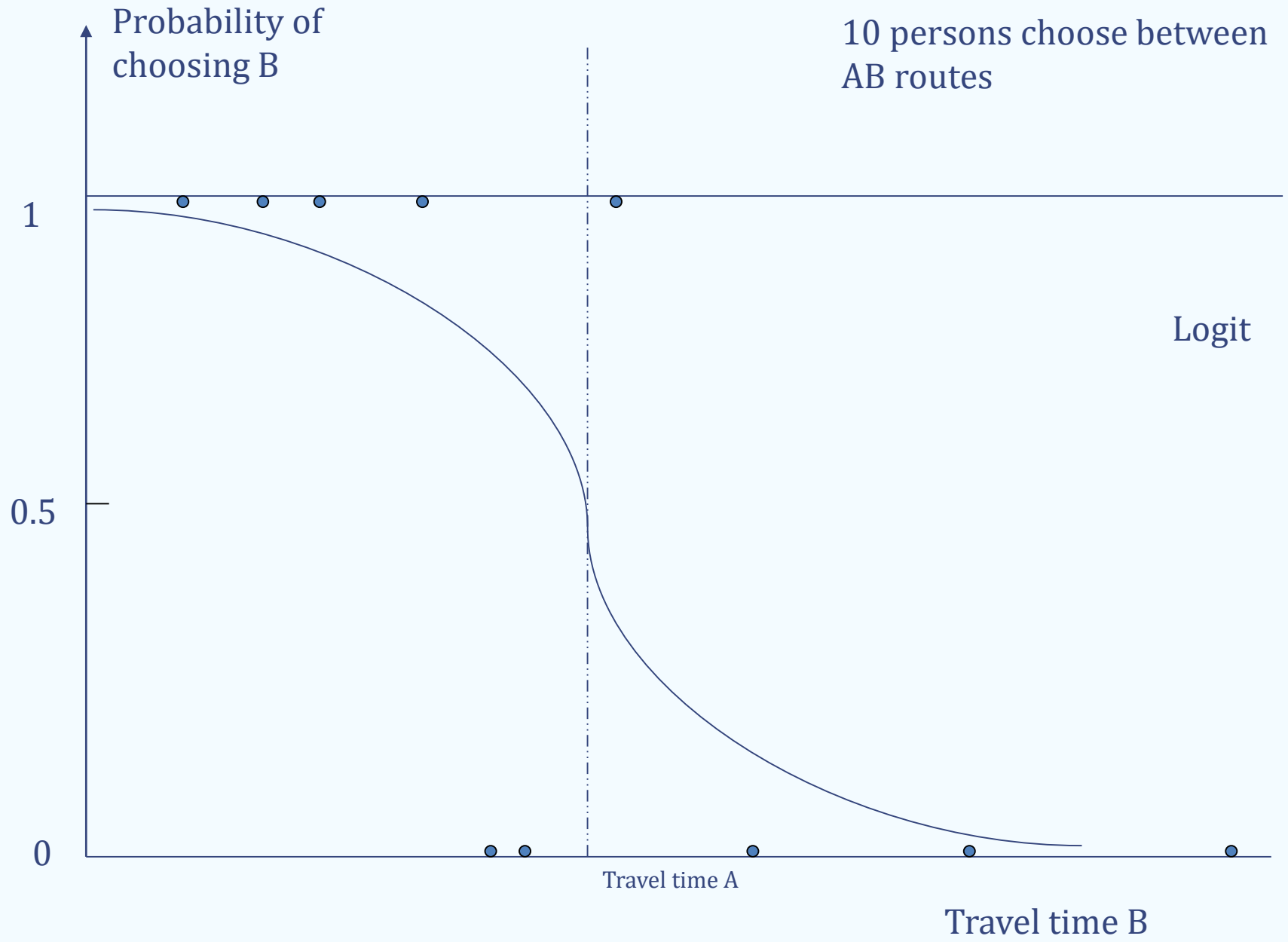
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- Consider you have 10 individuals that choose between two routes A en B
- Travel time of A is 9 and of B is 10 minutes
- Some people take route B
 - E.g. because they like particular features of , or they misjudge the travel time

- Let's do a regression of whether or not you have chosen B on the difference between the travel time of A and B :
$$y_B = f(\alpha + \beta(\text{travel time}_B - \text{travel time}_A)) + \epsilon$$
where $y_B = 1$ if you choose B and zero otherwise







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- **Indirect utility may be given by:**

$$U_{iA} = V_A(\text{travel time}_A) + \epsilon_{iA} \quad (2)$$

$$U_{iB} = V_B(\text{travel time}_B) + \epsilon_{iB} \quad (3)$$

- $V_A, V_B \rightarrow$ **deterministic utility**

- **Random terms: $\epsilon_{iA}, \epsilon_{iB}$: random taste variation**

- **Random utility model (RUM)**
- **Note that the levels of U_{iA} and U_{iB} are not directly observed!**

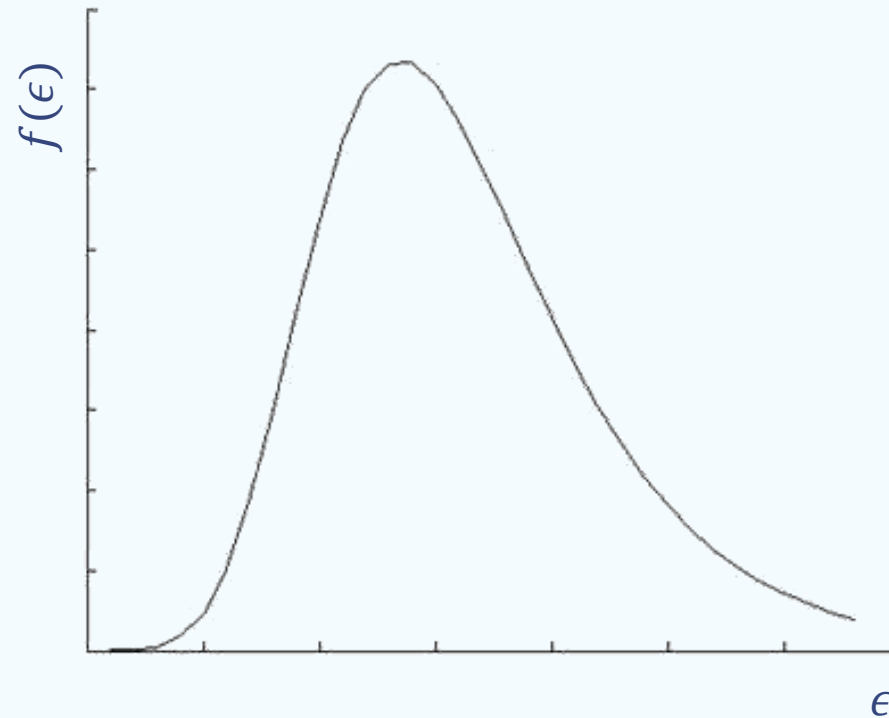
- $\Pr(Y = A) = \Pr(U_{iA} > U_{iB})$
- $\Pr(V_A + \epsilon_{iA} > V_B + \epsilon_{iB}) = \Pr(V_A - V_B > \epsilon_{iB} - \epsilon_{iA})$

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- **Two things are unknown**
 - **Which distribution for ϵ 's?**
 - **What is the functional form for V_A and V_B ?**

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- Which distribution for ϵ 's?
 - ϵ 's are unobserved
 - You draw them from a distribution
 - Logit: Extreme Value Type I distribution



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- Which distribution for ϵ 's?
 - Extreme Value Type I distribution
 - Generates simple closed-form solutions!
 $\rightarrow \Pr(V_A - V_B > \epsilon_{iB} - \epsilon_{iA})$
 - Daniel McFadden (1964)



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- **It appears that:**

$$\Pr(Y = A) = \frac{e^{V_A}}{e^{V_A} + e^{V_B}} \quad (4)$$

- **With two alternatives this can be written as:**

$$\Pr(Y = A) = \frac{1}{1 + e^{V_B - V_A}}$$

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- Which functional form for V_A and V_B ?

- Can be any function
- Linear function is often assumed
- Can be extended with multiple variables

$$U_{jA} = \beta p_{jA} + \kappa t_{jA} + \epsilon_{jA} \quad (5)$$

$$U_{jB} = \beta p_{jB} + \kappa t_{jB} + \epsilon_{jB} \quad (6)$$

where p_{jA} is the price of a trip and t_{jA} is travel time of alternative j

- $\beta < 0, \kappa < 0$

- Recall (from previous slide):

- $$\Pr(Y = A) = \frac{1}{1 + e^{\beta(p_{jB} - p_{jA}) + \kappa(t_{jB} - t_{jA})}}$$

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- **Important concept in Transport Economics:**
Value of Time (VOT)
 - “How much are you willing to pay to reduce your travel time with one hour, *holding utility constant*”

- **Let's take the deterministic utility function**
$$U_{jA} = \beta p_{jA} + \kappa t_{jA} + \varepsilon_{jA} \quad (7)$$

- **When t_{jA} is measured in hours, the VOT can be written as κ/β**

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- Value of time is often used in cost benefit analyses
- VOT depends on trip purpose
 - Business €26.25/h
 - Commuting €9.25/h
 - Social purpose €7.50/h
- VOT depends on income
 - About 50% of net income

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- **The choice probability for two alternatives:**

$$\Pr(Y = A) = \frac{e^{\beta x_A}}{e^{\beta x_A} + e^{\beta x_B}}$$

- **Usually there are more alternatives in the choice set**

- Train, bus, car
- Rotterdam, Antwerp, Hamburg
- Routes to the VU

- **Simply extend the logit formula:**

$$\Pr(Y = A) = \frac{e^{\beta x_A}}{e^{\beta x_A} + e^{\beta x_B} + e^{\beta x_C}}$$

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- The aggregate utility derived from the choice set is summarised by the logsum:

$$E[CS] = \frac{1}{v} \ln(e^{\beta x_A} + e^{\beta x_B} + e^{\beta x_C})$$

- v is the marginal utility of income
 - Can be used in welfare estimates
-
- Assume $\beta x_A = \beta x_B = 10$
 - Now alternative C is added and $\beta x_C = 1$
 - The average utility per alternative decreases from 10 to 7 but $E[CS]$ increase
 - ‘Love of variety’ effect

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- **Property of logit formula:**
 - **The *ratios* of choice probabilities for A and B do not depend on whether or not C is in the choice set**
 - **Independence of irrelevant alternatives**

- $$\frac{\Pr(Y=A)}{\Pr(Y=B)} = \frac{\left(\frac{e^{\beta x_A}}{e^{\beta x_A} + e^{\beta x_B} + e^{\beta x_C}} \right)}{\left(\frac{e^{\beta x_B}}{e^{\beta x_A} + e^{\beta x_B} + e^{\beta x_C}} \right)} = \frac{e^{\beta x_A}}{e^{\beta x_B}}$$

- **Let's find out whether this is a desirable property...**

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- **'The *Red Bus-Blue Bus*' problem**

- **Choice set 1: Train, red bus, blue bus**

- **Assume market shares are 70, 15 and 15%**

	Train	Red bus	Blue bus
V	2.54	1	1
Prob	0.700	0.150	0.150

- **Choice set 2: Train, red bus, so:**

	Train	Red bus
V	2.54	1
Prob	0.823	0.177

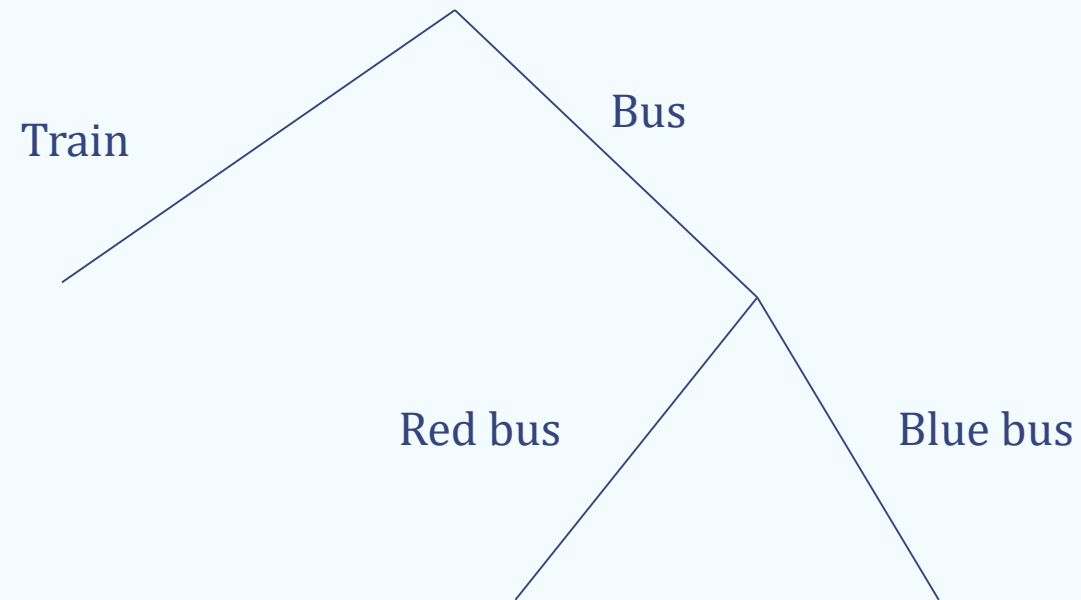
- **Probability to take the bus in choice set 2 is**

$$\frac{e^1}{e^{2.54} + e^1} = 0.177$$

- **Higher probability – not very realistic as red buses and blue buses are identical**

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- **So, when some alternatives are more similar than other alternatives, the use of multinomial choice model may be misleading**
- **Use nested logit!**



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- **Nested logit takes into account correlation between alternatives**
 - **But define nests yourself!**

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- **Let us define utility as follows:**

$$U_{jg} = V_j + W_g + \epsilon_{jg}$$

V_j only differs within nests between alternatives j

W_g only differs between nests g

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- **We may write the probability to choose an alternative:**

- $\Pr(d_j = 1) = \Pr(g) \cdot \Pr(j | g)$

- $\Pr(j | g) = \frac{e^{V_j/\lambda_g}}{\sum_{k \in g} e^{V_k/\lambda_g}}$

- $\Pr(g) = \frac{e^{W_g + \lambda_g I_g}}{\sum_{\tilde{g}} e^{W_{\tilde{g}} + \lambda_{\tilde{g}} I_{\tilde{g}}}}$

with $I_g = \log(\sum_{j \in g} e^{V_j/\lambda_g})$

- $\lambda_g = 1 \Rightarrow$ **no correlation (multinomial logit)**
- $\lambda_g \rightarrow 0 \Rightarrow$ **perfect correlation (red bus/blue bus)**

- **Hence, when j and k are in the same nest:**

$$\frac{\Pr(d_j = 1)}{\Pr(d_k = 1)} = \frac{e^{W_g + V_j/\lambda_g}}{e^{W_g + V_k/\lambda_g}} = \frac{e^{W_g + V_j}}{e^{W_g + V_k}} = \frac{e^{V_j}}{e^{V_k}}$$

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- So, nested logit probability depends on
 - Probability to choose a nest
 - Probability to choose an alternative within the nest

- Note that Nested Logit does not imply a *sequential* choice

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Today:

- **How to deal with a binary dependent variable?**

- **Links to economic theory with random taste variation**
 - **Random utility model**
 - **Assume distribution of ϵ_i**
 - **Extreme Value Type I is convenient**

- **Stated choice experiments can measure value of time**

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Tomorrow:

- **How to estimate binary choice models?**
 - Use LPM, Logit or Probit

- **Application to measure value of time, value schedule delay early and schedule delay late**

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Discrete choice (2)

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- **This week**
 - **Learn about how to deal with discrete choices**
 - **... and stated choice experiments**

- **Plan:**
 - Lecture #1: The random utility framework
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- **How to estimate binary discrete choice models?**
- **Three main options**
 1. **Linear probability model**
 2. **Logit**
 3. **Probit**

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- **Regress 0/1 variable on characteristics of that choice and use OLS:**

$$\Pr(d_j = 1) = \beta' x_j$$

- **Dataset example:**

Chosen	Price	Time
1	14	12
0	25	5
0	15	15
1	15	13
1	4	45
1	3	40
0	20	10

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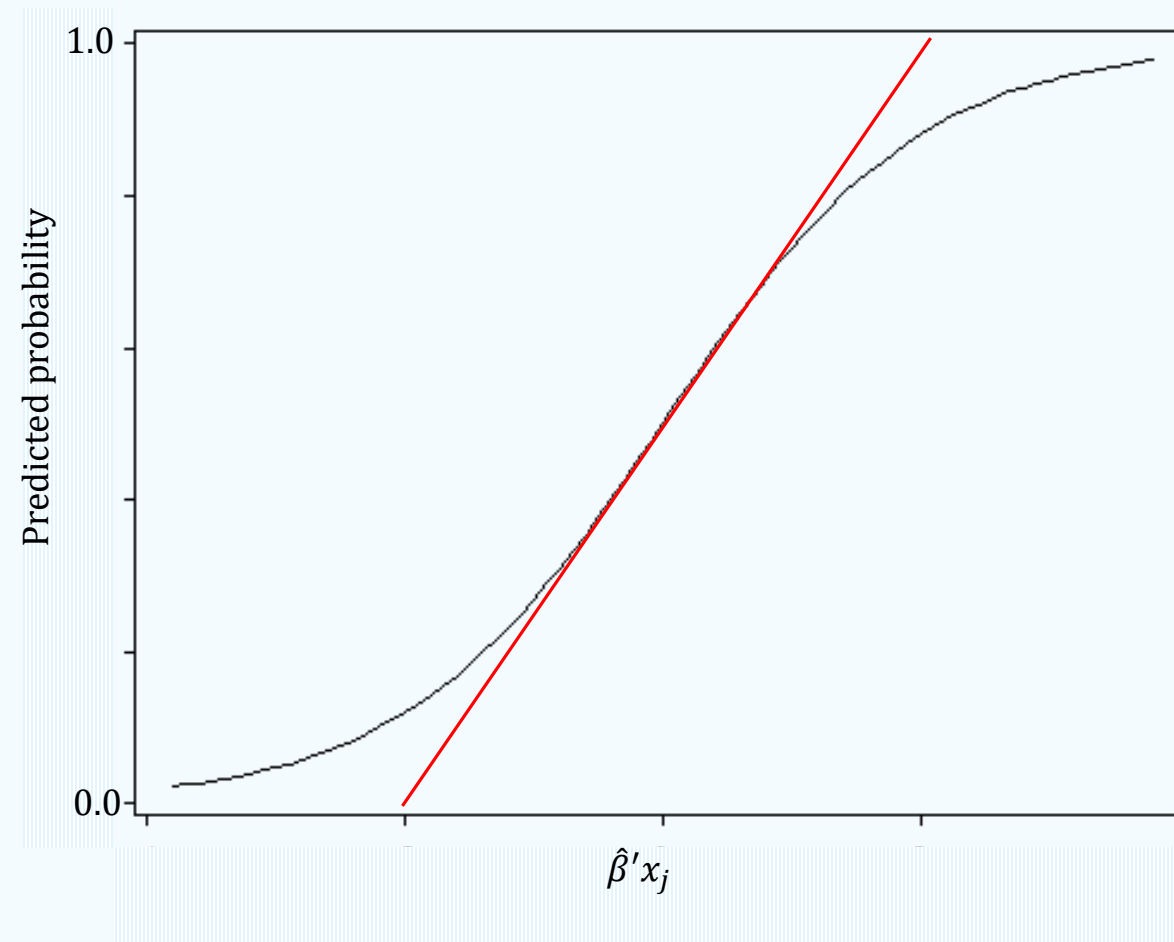
Advantages:

- Consistent when $0 \leq \hat{y}_j \leq 1 \forall j$

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Advantages:

- Consistent when $0 \leq \hat{y}_j \leq 1 \forall j$



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Advantages:

- **Consistent when $0 \leq \hat{y}_j \leq 1 \forall j$**
- **Easy to interpret**
 - **Say that $\beta = -0.25$ and x is measured in €, then for each euro increase in x , the probability to choose alternative j decreases by 25 percentage points**
 - $$\frac{\partial \Pr(d_{j=1})}{\partial x} = \beta$$

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Advantages:

- **Consistent when $0 \leq \hat{y}_j \leq 1 \forall j$**
- **Easy to interpret**
 - $\frac{\partial \Pr(d_j=1)}{\partial x} = \beta$
- **Computationally feasible**
 - **Important for large panel datasets**
- **In practice, leads to very similar results as Logit and Probit**

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Disadvantages:

- **No direct link with structural parameters of utility function**
 - e.g. not able to calculate aggregate utility from choice set

- **Biased for small samples and possibly inconsistent marginal effects**
 - **Linearity?**

- **Not suitable for multinomial choices**

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- **Let's define**

$$\Pr(d_j = 1) = \frac{1}{1 + e^{-\beta'x_j}}$$

- **Example: regress 0/1 variable on *differences* in characteristics of the alternatives**

Chosen _B	Price _B -Price _A	Time _B -Time _A
1	-14	5
0	5	0
0	15	-20
1	-8	13
1	-10	3
1	3	-5
0	20	10

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- **Recall**

- $\Pr(d_j = 1) = \left(1 + e^{-\beta'x_j}\right)^{-1}$

- **The change in the probability for one unit increase in x**

- $\frac{\partial \Pr(d_j=1)}{\partial x_j} = \beta \frac{e^{-\beta'x_j}}{(1+e^{-\beta'x_j})^2}$

- **Marginal effect depends on x_j , so is not constant/linear**

- For example, evaluate at mean values of x

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- **Marginal effects:**

- **Use chain rule of differentiation**

- $$\frac{\partial \Pr(d_j=1)}{\partial x_j} = -\left(1 + e^{-\beta'x_j}\right)^{-2} \times e^{-\beta'x_j} \times -\beta$$

- $$\frac{\partial \Pr(d_j=1)}{\partial x_j} = \beta \frac{e^{-\beta'x_j}}{(1+e^{-\beta'x_j})^2}$$

- **Dependent on x_j , so is not constant/linear**

- **For example, evaluate at mean values of x**

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- **Software**
 - LOGIT **or** LOGISTIC **in STATA**
 - REGRESSION – BINARY LOGISTIC **in SPSS**

- **In STATA you can select to report marginal effects**
 - **Use MARGINS after LOGIT command**
 - **Choose at which x the values are evaluated (e.g. at means)**

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Advantages of Logit:

- **Predicted probability is always between one and zero**
- **Clear link to random utility framework**
 - **Log-sum may be used for welfare calculations**
- **Closed-form marginal effects**
 - **Usually leads to very similar results as Probit**
- **Can include ‘fixed effects’ (XTLOGIT in STATA)**
 - *e.g. to control for individual heterogeneity*

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Disadvantages of Logit:

- **Why Extreme Value Type I distribution for ϵ ?**

- **Maximum likelihood / non linear model**

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- We may also assume that ϵ_j is normally distributed, so $\epsilon_j = N(0, \sigma^2)$
 - This implies $\Pr(d_j = 1) = \Phi(\beta' x_j)$
 - Central limit theorem?
 - However, no closed-form for cumulative normal distribution!

- Marginal effects:

$$\frac{\partial \Pr(d_j=1)}{\partial x_j} = \beta \phi(\beta x_j)$$

where $\phi(\cdot)$ is the density function of the normal distribution

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Advantages:

- Normal distribution for ϵ_j seems reasonable
 - ... Central limit theorem
- Probability is always between one and zero

Disadvantages:

- No closed-form marginal effects
- Hard to include many fixed effects

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- **How to choose between the three models?**
 - **Probit estimates \approx Logit estimates**
 - **Look at goodness of fit**
 - Use $|d_j - \hat{d}_j|$
 - **Check for robustness of marginal effects**
 - **Large sample and interested in marginal effects?**
 - **Usually linear probability model!**
 - **There is an ongoing debate in economics on this issue**

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Today:

- **How to estimate binary choice models?**
 - **Use LPM, Logit or Probit**

- **Application to measure value of time, value schedule delay early and schedule delay late**

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Tomorrow:

- **Generalisations of logit models**
 - **Multinomial logit**
 - **Nested logit**
- **Conditional logit models**
 - **Poisson regression**
- **Data**
 - **Stated preference or revealed preference data**

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Discrete choice (3)

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- **This week**
 - **Learn about how to deal with discrete choices**
 - **... and stated choice experiments**

- **Plan:**
 - Lecture #1: The random utility framework
 - Lecture #2: Estimating binary choice models
 - Lecture #3: Estimating multinomial choice models**
Stated vs. revealed preference data
 - Assignment: Estimate the value of time**

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- **How to estimate these types of models?**

- **Overview**

	# Alternatives	Coefficients
1. Binary Logit	2	Homogeneous
2. Multinomial Logit with alternative specific parameters	>2, <~10	Differ between alternatives
3. Nested Logit	>2, <~10	Usually homogeneous
4. Conditional Logit	>2	Homogeneous

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- **Recall:**

$$\Pr(Y = A) = \frac{e^{\beta x_A}}{e^{\beta x_A} + e^{\beta x_B} + e^{\beta x_C}}$$

But now let the coefficients be alternative-specific:

$$\Pr(Y = A) = \frac{e^{\beta_A x_A}}{e^{\beta_A x_A} + e^{\beta_B x_B} + e^{\beta_C x_C}}$$

- **We cannot identify all the coefficients $\beta_A, \beta_B, \beta_C$, because we compare the results to a reference category**
 - » **Think of dummies**
- **Illustration: we can write the probability only in terms of differences with respect to one reference category, e.g.:**

$$\Pr(Y = A) = \frac{1}{1 + e^{\beta_B x_B - \beta_A x_A} + e^{\beta_C x_C - \beta_A x_A}}$$

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- **What demographic factors explain car ownership?**
 - $0 = \text{no car}; 1 = 1 \text{ car}; 2 \geq 1 \text{ car}$

- **Data, $n=55958$**

respid	carown	hhsiz	children	...	socallow
100001	1	4	1	...	0
100002	2	2	0	...	0
100004	0	2	0	...	1
100005	1	2	0	...	0
100012	2	5	1	...	0
...
622410	2	3	1	...	0

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- **What demographic factors explain car ownership?**
- **Start with OLS**
 - **... but car ownership is not really a continuous variable in the data**

Table – EXPLAINING CAR OWNERSHIP
(Dependent variable: The number of cars in the household)

	coeff.	s.e.
Household size	0.1745***	(0.0069)
Number of children in the household	-0.0045	(0.0163)
Social allowance (=1)	-0.6624***	(0.0120)
Male (=1)	0.1093***	(0.0051)
Age	-0.0031***	(0.0002)
Long term illness (=1)	-0.1317***	(0.0060)
Constant	0.7270***	(0.0152)
Number of observations	55,958	
R^2	0.2145	

Notes: Robust standard errors are in parentheses. *** $p < 0.01$, ** $p < 0.05$, * $p < 0.10$.

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■ *MLOGIT YVAR XVARS , BASEOUTCOME(0)*

Table – EXPLAINING CAR OWNERSHIP

Outcome = 0 (base outcome)	coeff.	s.e.
Outcome = 1	coeff.	s.e.
Household size	1.0039***	(0.0196)
Number of children in the household	-0.8290***	(0.0445)
Social allowance (=1)	-2.1039***	(0.0596)
Male (=1)	0.4870***	(0.0233)
Age	-0.0043***	(0.0007)
Long term illness (=1)	-0.3917***	(0.0248)
Constant	-0.6280***	(0.0506)
Outcome = 2	coeff.	s.e.
Household size	1.3039***	(0.0222)
Number of children in the household	-0.5191***	(0.0522)
Social allowance (=1)	-4.7724***	(0.2219)
Male (=1)	0.5910***	(0.0295)
Age	-0.0171***	(0.0009)
Long term illness (=1)	-0.7218***	(0.0358)
Constant	-1.9361***	(0.647)
Number of observations	55,958	
Log-likelihood	-48,268	
Pseudo R^2	0.1333	

Notes: Standard errors are in parentheses. *** $p < 0.01$, ** $p < 0.05$, * $p < 0.10$.

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- All the coefficients are compared to one base category!
- Coefficients are different for different alternatives
- Particularly useful when outcomes do not have a logical ordering
 - Bus, car, train
 - Holiday destinations
 - Otherwise: OLS or Ordered Logit
- If the number of alternatives is very large → too many coefficients to interpret meaningfully

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- **Independence of irrelevant alternatives**
 - **Adding an alternative does not affect the relative odds between two other options considered**
 - **Solution: use Nested Logit**
 - **Allows for correlation within nests**

- **Software**
 - **NLOGIT in STATA**
 - **Use Biogeme software**
 - **Limdep/nlogit**

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- **Often, the number of alternatives is very large**
 - Location choice
 - Route choice
 - Holiday destinations
 - Choice of car
 - Partner choice
 - ...

- **With Multinomial Logit this becomes infeasible**
 - Unique coefficients for each alternative
 - Not necessary for large choice sets

- **Conditional Logit:**

$$\Pr(d_j = 1) = \frac{e^{\beta' x_j}}{\sum_{k=1}^J e^{\beta' x_k}}$$

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- **How to deal with large choice sets?**
 - **Number of observations in your regressions is *number of alternatives* \times *respondents***

1. **Model aggregate choices**
2. **Random selection of alternatives**
3. **Estimate count data models (Poisson)**

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1. Model aggregate choices

- **Modelling location choice**
 - **Focus on aggregate areas (municipalities)**
- **Choice of cars**
 - **Only distinguish between brands**
- **However, lack of detail makes results less credible**

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2. Random selection of alternatives

- **McFadden (1978)**
 - Choose a random subset of J alternatives for each choice set, including the chosen option
 - This should not affect the *consistency* of the estimated parameters
 - Small-sample properties are yet unclear

- **How large should J be?**

- **Applied in many good papers**
 - e.g. Bayer et al. (2007, *JPE*)

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3. Estimate count data models

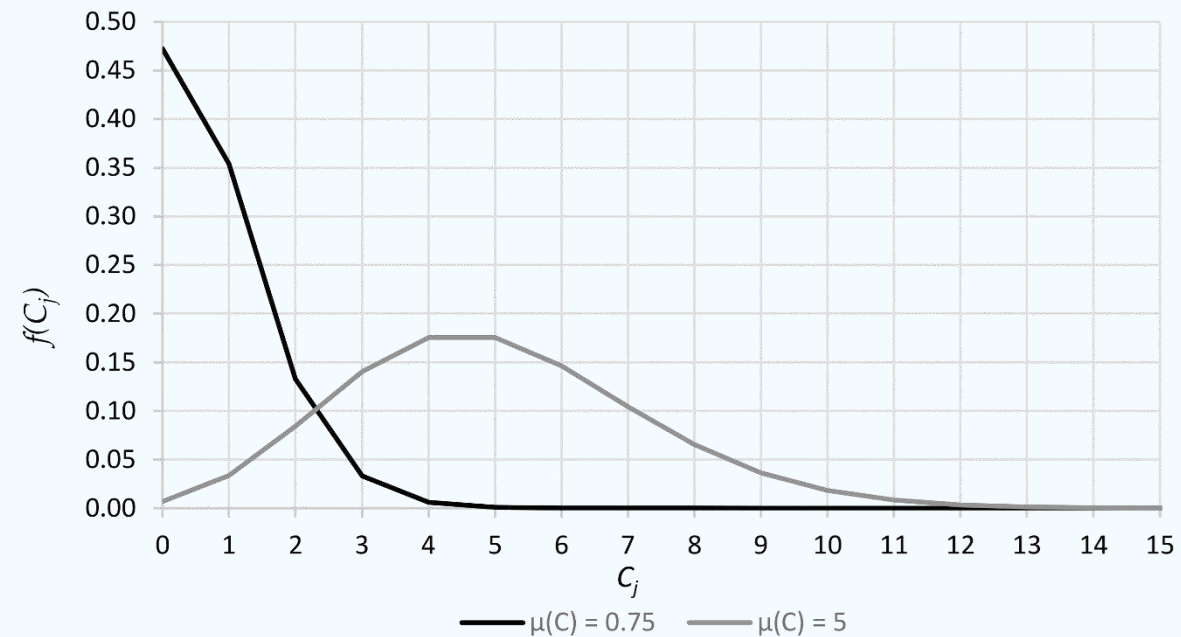
- Estimate Conditional Logit by means of a Poisson model

- A Poisson regression is a count data model
 - Dependent variable is integer
 - ... and should be Poisson distributed

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3. Estimate count data models

- Example of a Poisson distribution



- Equidispersion: $\bar{y} = \sigma_y$

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3. Estimate count data models

- **Estimate Conditional Logit by means of a Poisson model**

- **A Poisson regression is a count data model**

- **Dependent variable is integer**
- **... and should be Poisson distributed**
- $C_j = e^{\beta' x_j} + \epsilon$

where C_j is the # of decision makers that have chosen a certain alternative

- **Convenient interpretation of β**

- **When x_j increases with one, C_j increases with $\beta \times 100$ percent**

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3. Estimate count data models

- **A Poisson model should give identical parameters to the Conditional Logit**
 - **Maximum likelihood functions are identical *up to a constant***
 - **Guimarães et al. (2003)**

- **Hence, group observations based on their chosen alternatives**
 - **... the number of firms choosing a certain location**
 - **... the number of people buying a certain car**

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3. Estimate count data models

- **Implications**

- You cannot include characteristics of the decision maker (*because you sum up all choices*)!
- Homogeneous parameters across the population

- **Extensions**

- Include fixed effects
- Negative binomial regression
- Zero-inflated models
- See Guimarães et al. (2004) for details

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Types of data

- Revealed preference (RP) data
 - Observed or reported actual behaviour

- Stated preference (SP) data
 - Respondents are confronted with hypothetical choice sets

- Combinations of RP and SP

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Advantages of RP data

- **Based on actual behaviour!!**
- **Use existing (large) data sources**
 - **Cheaper**
 - **No expensive experiments**
- **Panels of the same individuals over a long time**

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Disadvantages of RP data

- **Lack of variability**
- **Collinearity (e.g. price and travel times)**
- **Lack of knowledge on the choice set**
- **Not possible with new choice alternatives**
- **Actual behaviour may not be first choice**
 - **University numerus fixus**
- **Perception errors and imperfect information**
 - **Airline tickets**

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- **Example of stated preference question**

Suppose you have to ship a product from A to B

Option 1		Option 2	
Price:	€ 1,000	Price:	€ 750
Handling time:	3 days	Handling time:	1 week
% does not arrive:	1.0%	% does not arrive:	1.3%
What alternative will you choose?			

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Advantages of SP data

- **New alternatives**
- **New attributes**
- **Large variability is possible**
- **Problems of collinearity can be solved**
 - **‘Orthogonal design’**
- **Choice set is clearly defined**

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Disadvantages of SP data

- **Information bias**
- **Starting point bias**
- **Hypothetical bias**
- **Strategic bias**
- **Errors**

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Disadvantages of SP data

- Information bias
 - The respondent has incorrect information on the context
 - Make your experiment as realistic as possible

- Starting point bias
 - Respondents are influenced by the set of available responses to the experiment
 - Test your design and choose realistic attribute values

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Disadvantages of SP data

- Hypothetical bias
 - Individuals tend to respond differently to hypothetical scenarios than they do to the same scenarios in the real world.
 - Cognitive incongruity with actual behaviour
 - Again: make your experiment as realistic as possible
 - But otherwise hard to mitigate...

- Strategic bias
 - Respondent wants a specific outcome
 - (S)he fills in answers that are in line with desired outcomes

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Disadvantages of SP data

- Unintentional biases
 - Information, starting point, hypothetical bias
- Intentional biases
 - Strategic bias
- Errors
 - Boredom
 - Respondents do not carefully read instructions
 - Respondents do not understand the questions

If there is good data available, I would prefer RP
(*personal opinion*)

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Today:

- **Generalisations of logit models**
 - **Multinomial logit**
 - **Nested logit**
 - **Conditional logit**

- **Conditional Logit models can be estimated by count data models**
 - **Cannot include characteristics of the decision maker**

- **Data**
 - **Stated preference or revealed preference data**

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Next week:

- **Identification of causal effects**